## Section 9.6 Answer

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 $\mathbf{2.} \ \, \mathrm{a.} \ \, \mathrm{cooperation.}$ 

b. competition.

4. a. See Figure 1.

At t = 0, there are about 600 rabbits and 160 foxes. At  $t = t_1$ , the number of rabbits reacher a minimum of 80 and the number of foxes is 80. At  $t = t_2$ , the number of foxes reaches a minimum, 25, while the number of rabbits rebounds to 1000. At  $t = t_3$ , the number of foxes increases to 40 and the number of rabbit reaches a maximum of about 1750. The curves ends at  $t = t_4$ , the numbers of foxes and rabbits are 65 and 95, respectively.

**b.** Figure 2.

## **6.** Figure 3.

8. a. solve 
$$\frac{dA}{dt} = 0$$
,  $\frac{dL}{dt} = 0$ .  
The we obtain  $(A, L) = (0, 0)$  or  $(5000, 200)$ .

b.

$$\frac{dL}{dA} = \frac{dL/dt}{dA/dt} = frac - 0.5L + 0.0001AL2A - 0.01AL.$$

c. Figure 4.

The solution curves are closed curves that have the equilibrium point (5000, 200).

**d.** Figure 5. At  $P_0(1000, 200)$ , dA/dt = 0 and dL/dt < 0, so the number of ladybugs is decreasing. At  $P_0$ , there aren't enough aphids to support the ladybug population, so the number of ladybugs decreases and the number of aphids begins to increase. The ladybug population reaches a minimum at  $P_1(5000, 100)$  while the aphid population increases in a dramatic way reaching its maximum at  $P_2(14250, 200)$ . Meanwhile, the ladybug population is increasing from  $P_1$  to  $P_3(5000, 355)$ , and as we pass through  $P_2$ , the increasing number of ladybugs starts to delete the aphid population. At  $P_3$ , the ladybugs reach a maximum population, and start to decrease due to the reduced aphid population. Both populations then decrease until  $P_0$ , where the cycle starts over again.



Figure 1:



Figure 2:

e. Figure 6.

Both graphs have the same period and the graph of L peaks about a quarter of a cycle after the graph of A.

10. a. If L = 0, A = 0 or 10000. Since dA/dt > 0 for 0 < A < 10000, the aphid population to increase to 10000 in the interval. Since dA/dt < 0 for A > 10000, the aphid population to decrease to 10000 in the interval. Hence, the aphid population to stabilize at 10000.

**b.** solve 
$$\frac{dA}{dt} = 0, \frac{dL}{dt} = 0.$$

The we obtain (A, L) = (0, 0), (10000, 0) or (5000, 100).

c.

$$\frac{dL}{dA} = \frac{dL/dt}{dA/dt} = frac - 0.5L + 0.0001AL2A(1 - 0.0001A) - 0.01AL.$$

d. Figure 7.

All of the phase trajectories spiral tightly around (5000, 100).

e. Figure 8.

At t = 0, the bug population decreases rapidly and the aphid population decreases slightly before beginning to increase. As the aphid population continues to increase, the bug population reaches a minimum at about (5000, 75). The gug population starts to increase





Figure 4:

and quickly stabilizes at 100, while the aphid population stabilizes at 5000.

**f.** Figure 9.

The graph of A peaks just after the graph of L has a minimum.



Figure 5:



Figure 6:



Figure 7:



Figure 8:



Figure 9: