

Section 3.1

$$7. f(x) = x^3 - 4x + 6 \Rightarrow f'(x) = 3x^2 - 4(1) + 0 = 3x^2 - 4$$

$$23. y = \frac{x^2 + 4x + 3}{\sqrt{x}} = x^{3/2} + 4x^{1/2} + 3x^{-1/2} \Rightarrow$$

$$y' = \frac{3}{2}x^{1/2} + 4\left(\frac{1}{2}\right)x^{-1/2} + 3\left(-\frac{1}{2}\right)x^{-3/2} = \frac{3}{2}\sqrt{x} + \frac{2}{\sqrt{x}} - \frac{3}{2x\sqrt{x}} \quad \left[\text{note that } x^{3/2} = x^{2/2} \cdot x^{1/2} = x\sqrt{x}\right]$$

$$\text{The last expression can be written as } \frac{3x^2}{2x\sqrt{x}} + \frac{4x}{2x\sqrt{x}} - \frac{3}{2x\sqrt{x}} = \frac{3x^2 + 4x - 3}{2x\sqrt{x}}.$$

$$32. y = e^{x+1} + 1 = e^x e^1 + 1 = e \cdot e^x + 1 \Rightarrow y' = e \cdot e^x = e^{x+1}$$

$$33. y = \sqrt[4]{x} = x^{1/4} \Rightarrow y' = \frac{1}{4}x^{-3/4} = \frac{1}{4\sqrt[4]{x^3}}. \quad \text{At } (1, 1), y' = \frac{1}{4} \text{ and an equation of the tangent line is}$$

$$y - 1 = \frac{1}{4}(x - 1) \text{ or } y = \frac{1}{4}x + \frac{3}{4}.$$

$$49. (a) s = t^3 - 3t \Rightarrow v(t) = s'(t) = 3t^2 - 3 \Rightarrow a(t) = v'(t) = 6t$$

$$(b) a(2) = 6(2) = 12 \text{ m/s}^2$$

$$(c) v(t) = 3t^2 - 3 = 0 \text{ when } t^2 = 1, \text{ that is, } t = 1 \text{ and } a(1) = 6 \text{ m/s}^2.$$