

32.

For the side of triangle from A to B, use  $(x_1, y_1) = (1, 1)$  and  $(x_2, y_2) = (4, 2)$ . Hence, the equation are

$$x = x_1 + (x_2 - x_1)t = 1 + (4 - 1)t = 1 + 3t,$$

$$y = y_1 + (y_2 - y_1)t = 1 + (2 - 1)t = 1 + t.$$

Graph it. 34.

(a) Let  $\frac{x^2}{a^2} = \sin^2 t$  and  $\frac{y^2}{b^2} = \cos^2 t$  to obtain  $x = a \sin t$  and  $y = b \cos t$  with  $0 \leq t \leq 2\pi$  as possible parametric equations for the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ .

(b) The equation are  $x = 3 \sin t$  and  $y = b \cos t$  for  $b \in \{1, 2, 4, 8\}$ .

(c) As  $b$  increase, the ellipse stretches vertically.

36. If you are using a calculator or computer that can overlay graphs(using multiple  $t$ -intervals), the following are appropriate.

*Leftside* :  $x = 1$  and  $y$  goes from 1.5 to 4, so use

$$x = 1, \quad y = t, \quad 1.5 \leq t \leq 4$$

*Rightside* :  $x = 10$  and  $y$  goes from 1.5 to 4, so use

$$x = 10, \quad y = t, \quad 1.5 \leq t \leq 4$$

*Bottom* :  $x$  goes from 1 to 10 and  $y = 1.5$ , so use

$$x = t, \quad y = 1.5, \quad 1 \leq t \leq 10$$

*Handle* : It starts at (10,4) and ends at (13,7), so use

$$x = 10 + t, \quad y = 4 + t, \quad 0 \leq t \leq 3$$

*Leftwheel* :It's centered at (3,1),has radius of 1,and appears to go about  $30^\circ$  above the horizontal, so use

$$x = 3 + \cos t, \quad y = 1 + \sin t, \quad \frac{5\pi}{6} \leq t \leq \frac{13\pi}{6}$$

*Rightwheel* :Similar to the left wheel with center (8,1), so use

$$x = 8 + \cos t, \quad y = 1 + \sin t, \quad \frac{5\pi}{6} \leq t \leq \frac{13\pi}{6}$$

38.

(a)  $x = t$ , so  $y = t^{-2} = x^{-2}$ . We get the entire curve  $y = \frac{1}{x^2}$  traversed in a left-to-right direction.

(b)  $x = \cos t$ ,  $y = \sec^2 t = \frac{1}{\cos^2 t} = \frac{1}{x^2}$ . Since  $\sec t \geq 1$ , we only get the parts of the curve  $y = \frac{1}{x^2}$  with  $y \geq 1$ . We get the first quadrant portion of the curve when  $x > 0$ , that is  $\cos t > 0$ , and we get the second quadrant portion of the curve when  $x < 0$ , that is,  $\cos t < 0$ .

(c)  $x = e^t$ ,  $y = e^{-2t} = x^{-2}$ . Since  $e^t$  and  $e^{-2t}$  are both positive, we only get the first quadrant portion of the curve  $y = \frac{1}{x^2}$ .

40. The first two diagram depict the case  $\pi < \theta < \frac{3\pi}{2}$ ,  $d < r$ . As in Example 6,  $C$  has coordinates  $(r\theta, r)$ . Now  $Q$  (in the second diagram) has coordinates  $(r\theta, r + d\cos(\theta - \pi)) = (r\theta, r - d\cos\theta)$ , so a typical point  $P$  of the trochoid has coordinates  $(r\theta + d\sin(\theta - \pi), r - d\cos\theta)$ . That is,  $P$  has coordinates  $(x, y)$ , where  $x = r\theta - d\sin\theta$  and  $y = r - d\cos\theta$ . When  $d = r$ , these equations agree with those of the cycloid.

42.

$A$  has coordinates  $(a\cos\theta, a\sin\theta)$ . Since  $OA$  is perpendicular to  $AB$ ,  $\triangle OAB$  is right triangle and  $B$  has coordinates  $(a\sec\theta, 0)$ . It follows that  $P$  has coordinates  $(a\sec\theta, b\sin\theta)$ . Thus, the parametric equations are  $x = a\sec\theta$ ,  $y = b\sin\theta$ .

44.

(a) Let  $\theta$  be the angle of inclination of segment  $OP$ . Then  $|OB| = \frac{2a}{\cos\theta}$ . Let  $C = (2a, 0)$ . Then by use of triangle  $OAC$  we see that  $|OA| = 2a\cos\theta$ . Now

$$|OP| = |AB| = |OB| - |OA| = 2a\left(\frac{1}{\cos\theta} - \cos\theta\right) = 2a\frac{1 - \cos^2\theta}{\cos\theta} = 2a\frac{\sin^2\theta}{\cos\theta} = 2a\sin\theta\cos\theta.$$

(b) Use the information and graph it.

46.

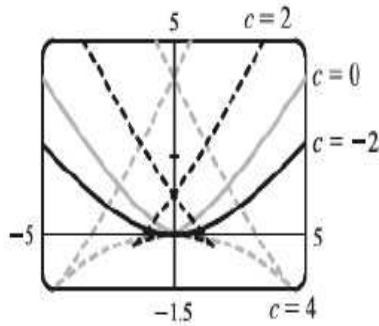
(a) If  $\alpha = 30^\circ$  and  $v_0 = 500\text{m/s}$ , then the equations become  $x = (500\cos 30^\circ)t = 250\sqrt{3}t$  and  $y = (500\sin 30^\circ)t - \frac{1}{2}(9.8)t^2 = 250t - 4.9t^2$ .  $y = 0$  when  $t = 0$  (when gun is fired) and again when  $t = \frac{250}{4.9} \approx 51\text{s}$ . Then  $x = (250\sqrt{3})\left(\frac{250}{4.9}\right) \approx$

22092m, so the bullet hits the ground about 22 km from the gun. The formula for  $y$  is quadratic in  $t$ .

(b) As  $\alpha(0^\circ < \alpha < 90^\circ)$  increases up to  $45^\circ$ , the projectile attains a greater height and a greater range. As  $\alpha$  increases pass  $45^\circ$ , the projectile attains a greater height, but its range decreases.

(c)  $x = (v_0 \cos \alpha)t \Rightarrow t = \frac{x}{v_0 \cos \alpha}$ . So  $y = (v_0 \sin \alpha)t - \frac{1}{2}gt^2 \Rightarrow y = (v_0 \sin \alpha)\frac{x}{v_0 \cos \alpha} - \frac{g}{2}\left(\frac{x}{v_0 \cos \alpha}\right)^2 = (\tan \alpha)x - \left(\frac{g}{2v_0^2 \cos^2 \alpha}\right)x^2$  which is the equation of a parabola (quadratic in  $x$ ).

48.



$x = 2ct - 4t^3$ ,  $y = -ct^2 + 3t^4$ . We use a graphing device to produce the graphs for various values of  $c$  with  $-\pi \leq t \leq \pi$ .

50. Use computer devices to plot some cases and observe their behavior.