

1. (10%) Find the equation of the tangent plane at the point $(1, 1, 0)$ to the surface $\ln xy + \sin yz = 0$.
2. (12%) Let $T(x, y, z) = \frac{80}{1 + x^2 + 2y^2 + 3z^2}$ be the temperature at the point (x, y, z) . In which direction does the temperature increase fastest at the point $(1, 1, -2)$. What is the maximum rate of increase?
3. (12%) Find all the local maxima, local minima, and saddle points of the function $f(x, y) = e^x(x^2 - y^2)$.
4. (14%) The flat elliptic plate $x^2 + 4y^2 \leq 1$ is heated so that the temperature at (x, y) is $T(x, y) = x^2 + 8y^2 - x$. Find the temperatures at the hottest and coldest points on the plate. Must use the Lagrange's multiplier method in the process.
5. (10%) Evaluate the integral $\iint_{\Omega} (x^2 + y^2) dA$, where Ω is the triangle with vertices $(0, 1)$, $(1, 0)$, $(1, 1)$.
6. (12%) Evaluate the integral $\int_0^1 \int_{y^{1/2}}^1 \frac{1}{1+x^3} dx dy$.
7. (15%) The region Ω seated on the Upper Half Plane, is enclosed by $r = 1 - \cos \theta$, $y = x$, $y = -x$. Compute the double integral $I = \iint_{\Omega} \frac{1}{\sqrt{x^2 + y^2}} dA$.
8. (15%) Evaluate the integral $\iint_{\Omega} \sqrt{x + 2y}(x - y) dA$, where the region Ω is enclosed by the lines $x - y = 0$, $x - y = 1$, $x + 2y = 0$ and $x + 2y = 1$.