Section 1.1 Four Ways to Represent a Function

4. The graphs of f and g are given.

   (a) State the values of $f(-4)$ and $g(3)$.

   (b) Which is larger, $f(-3)$ or $g(-3)$?

   (c) For what values of x is $f(x) = g(x)$?

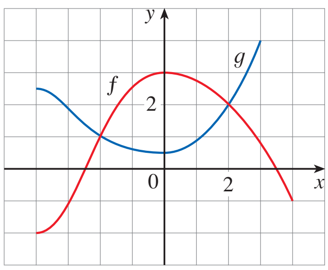
   (d) On what interval(s) is $f(x) \leq g(x)$?

   (e) State the solution of the equation $f(x) = -1$.

   (f) On what interval(s) is g decreasing?

   (g) State the domain and range of f.

   (h) State the domain and range of g.



Solution:

(a) From the graph, we have $f(-4) = -2$ and $g(3) = 4$.

(b) Since $f(-3) = -1$ and $g(-3) = 2$, or by observing that the graph of g is above the graph of f at $x = -3$, $g(-3)$ is larger than $f(-3)$.

(c) The graphs of f and g intersect at $x = -2$ and $x = 2$, so $f(x) = g(x)$ at these two values of x.

(d) The graph of f lies below or on the graph of g for $-4 \leq x \leq -2$ and for $2 \leq x \leq 3$. Thus, the intervals on which $f(x) \leq g(x)$ are $[-4, -2]$ and $[2, 3]$.

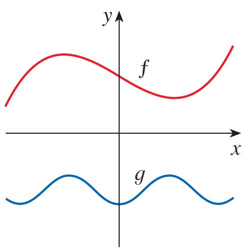
(e) $f(x) = -1$ is equivalent to $y = -1$, and the points on the graph of f with y-values of -1 are $(-3, -1)$ and $(4, -1)$, so the solution of the equation $f(x) = -1$ is $x = -3$ or $x = 4$.

(f) For any $x_1 < x_2$ in the interval $[-4, 0]$, we have $g(x_1) > g(x_2)$. Thus, $g(x)$ is decreasing on $[-4, 0]$.

(g) The domain of f is $\{x \mid -4 \leq x \leq 4\} = [-4, 4]$. The range of f is $\{y \mid -2 \leq y \leq 3\} = [-2, 3]$.

(h) The domain of g is $\{x \mid -4 \leq x \leq 3\} = [-4, 3]$. Estimating the lowest point of the graph of g as having coordinates $(0, 0.5)$, the range of g is approximately $\{y \mid 0.5 \leq y \leq 4\} = [0.5, 4]$.

78. Graphs of f and g are shown. Decide whether each function is even, odd, or neither. Explain your reasoning.



Solution:

f is not an even function since it is not symmetric with respect to the y-axis. f is not an odd function since it is not symmetric about the origin. Hence, f is *neither* even nor odd. g is an even function because its graph is symmetric with respect to the y-axis.