Possible correction to Problem 2. Try  $u = xy(\ln r)^{\beta+2}$  with  $r = (x^2 + y^2)^{1/2}$  and  $0 < \beta < 1$ . Sorry, I didn't do the detailed computations. If this doesn't work, please skip this problem. You could turn in the homework tomorrow.