

Institute of Mathematics Academia Sinica Department of Mathematics National Taiwan University



## Lakeside Lectures

## Speaker: Prof. Mei-Chi Shaw (蕭美琪) (Notre Dame University)

**Title:** Hearing Pseudoconvexity in Complex Manifolds



## Abstract:

The Cauchy-Riemann equations are fundamental in one and several complex variables. Holomorphic functions, for example, satisfy the homogeneous Cauchy-Riemann equations. In complex Euclidean space of dimension  $n \ge 2$ , the necessary and sufficient condition for the solvability of the Cauchy-Riemann equations is that the domain is pseudoconvex.

In this talk we relate pseudoconvexity with the vanishing of  $L^2$  Dolbeault cohomology groups. On a pseudoconvex domain in a complex manifold, the  $L^2$  Dolbeault cohomology might not even be Hausdorff. Recent results on the  $L^2$  closed range property for  $\overline{\partial}$  on an annulus between two pseudoconvex domains will be discussed. One can even characterize such domains through the spectral theory of their  $L^2$  Dolbeault cohomology groups, thus hearing pseudoconvexity of the boundary.

(Joint work with Debraj Chakrabarti, Siqi Fu, and Christine Laurent-Thiébaut).

Date: Jan. 15 (Mon), 2018

Time: 14:00-15:00

Venue: Room 202, Astro-Math Building (NTU Campus)

Refreshment: 13:30

Organizers: I-Kun Chen, Volker Elling, Chun-Yen Shen